

# Quantifying Defects in Graphene via Raman Spectroscopy at Different Excitation Energies

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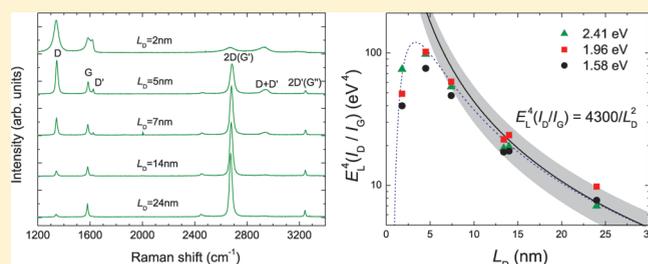
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**ABSTRACT:** We present a Raman study of Ar<sup>+</sup>-bombarded graphene samples with increasing ion doses. This allows us to have a controlled, increasing, amount of defects. We find that the ratio between the D and G peak intensities, for a given defect density, strongly depends on the laser excitation energy. We quantify this effect and present a simple equation for the determination of the point defect density in graphene via Raman spectroscopy for any visible excitation energy. We note that, for all excitations, the D to G intensity ratio reaches a maximum for an interdefect distance  $\sim 3$  nm. Thus, a given ratio could correspond to two different defect densities, above or below the maximum. The analysis of the G peak width and its dispersion with excitation energy solves this ambiguity.



**KEYWORDS:** Graphene, defects, Raman spectroscopy, excitation energy

Quantifying defects in graphene related systems, which include a large family of  $sp^2$  carbon structures, is crucial both to gain insight in their fundamental properties and for applications. In graphene this is a key step toward the understanding of the limits to its ultimate mobility.<sup>1–3</sup> Significant efforts have been devoted to quantify defects and disorder using Raman spectroscopy for nanographites,<sup>4–20</sup> amorphous carbons,<sup>18–24</sup> carbon nanotubes,<sup>25,26</sup> and graphene.<sup>11,27–35</sup> The first attempt was the pioneering work of Tuinstra and Koenig.<sup>4</sup> They reported the Raman spectrum of graphite and nanocrystalline graphite and assigned the mode at  $\sim 1580$   $\text{cm}^{-1}$  to the high frequency  $E_{2g}$  Raman allowed optical phonon, now known as G peak.<sup>5</sup> In defective and nanocrystalline samples they measured a second peak at  $\sim 1350$   $\text{cm}^{-1}$ , now known as D peak.<sup>5</sup> They assigned it to an  $A_{1g}$  breathing mode at the Brillouin Zone (BZ) boundary  $K$ , activated by the relaxation of the Raman fundamental selection rule  $\mathbf{q} \approx 0$ , where  $\mathbf{q}$  is the phonon wavevector.<sup>4</sup> They noted that the ratio of the D to G intensities varied inversely with the crystallite size,  $L_a$ . Reference 18 noted the failure of the Tuinstra and Koenig relation for high defect densities and proposed a more complete amorphization trajectory valid to date. References 7, 8, 18, and 19 reported a significant laser excitation energy,  $E_L$ , dependence of the intensity ratio. References 9 and 10 measured this excitation laser energy dependency in the Raman spectra of nanographites, and the ratio between the D and G bands was shown to depend on  $E_L^4$ .

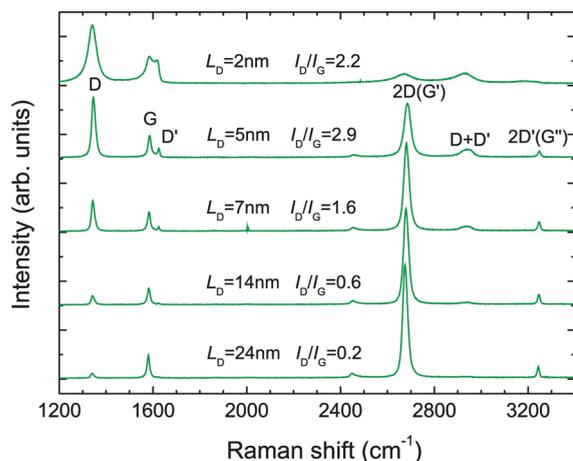
There is, however, a fundamental geometric difference between defects related to the size of a nanocrystallite and point defects in the  $sp^2$  carbon lattices, resulting in a different intensity ratio dependence on the amount of disorder. Basically, the amount of disorder in a nanocrystallite is given by the amount of border (one-dimensional defects) with respect to the total crystallite area, and this is a measure of  $L_a$ . In graphene with zero-dimensional pointlike defects, the distance between defects,  $L_D$ , is a measure of the amount of disorder, and recent experiments show that different approaches must be used to quantify  $L_D$  and  $L_a$  by Raman spectroscopy.<sup>28</sup> The effect of changing  $L_D$  on peak width, frequency, intensity, and integrated area for many Raman peaks in single layer graphene was studied in ref 29 and extended to few layer graphene in ref 30 all using a single laser line  $E_L = 2.41$  eV.

Here, to fully accomplish the protocol for quantifying pointlike defects in graphene using Raman spectroscopy (or equivalently,  $L_D$ ), we use different excitation laser lines in ion-bombarded samples and measure the D to G peak intensity ratio. This ratio is denoted in literature as  $I_D/I_G$  or  $I(D)/I(G)$ , while the corresponding area ratio, i.e., frequency integrated intensity ratio, as  $A_D/A_G$  or  $A(D)/A(G)$ . In principle, for small disorder or perturbations, one should always consider the area ratio, since the area under each peak represents the probability of the whole

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**Figure 1.** Raman spectra of five ion bombarded SLG measured at  $E_L = 2.41$  eV ( $\lambda_L = 514.5$  nm). The  $L_D$  are independently measured following the procedure of ref 28 and outlined in the main text. The main Raman peaks are labeled. The respective  $I_D/I_G$  values are indicated for each spectrum. The notation within parentheses [e.g.,  $2D(G')$ ] indicate two commonly used notations for the same peak ( $2D$  and  $G'$ ).<sup>31,43</sup>

process, considering uncertainty.<sup>29,36</sup> However, for large disorder it is far more informative to decouple the information on peak intensity and full width at half-maximum. The latter, denoted in literature as FWHM or  $\Gamma$ , is a measure of structural disorder,<sup>10,22,29</sup> while the intensity represents the phonon modes/molecular vibrations involved in the most resonant Raman processes.<sup>18,19,22</sup> For this reason, in this paper we will consider the decoupled  $I_D/I_G$  and peak widths trends. We find that, for a given  $L_D$ ,  $I_D/I_G$  increases as the excitation laser energy increases. We present a set of empirical formulas that can be used to quantify the amount of pointlike defects in graphene samples with  $L_D \geq 10$  nm using any excitation laser energy/wavelength in the visible range. The analysis of the D and G peak widths and their dispersions with excitation energy unambiguously discriminate between the two main stages of disordering incurred by such samples. We note that, by definition, our analysis only applies to defects able to activate the D peak in the Raman process. For example, it is well-known that perfect zigzag edges do not give rise to a D peak,<sup>32,33</sup> so a set of samples with an increasing amount of ideal zigzag edges would have a constant D peak, determined by other defects.

We produce single layer graphene (SLG) samples with increasing defect density by mechanical exfoliation followed by  $Ar^+$ -bombardment, as for the procedure outlined in ref 28. The ion-bombardment experiments are carried out in an OMICRON VT-STM ultrahigh vacuum system (base pressure  $5 \times 10^{-11}$  mbar) equipped with an ISE 5 Ion Source. The  $Ar^+$  ions have 90 eV kinetic energy and form an incidence angle of  $45^\circ$  with respect to the normal direction of the sample's surface. According to theoretical calculations, single and double vacancies in the graphene lattice are produced under these conditions.<sup>37,38</sup> Raman spectra are measured at room temperature with a Renishaw microspectrometer. The spot size is  $\sim 1 \mu m$  for a  $100\times$  objective, and the power is kept at  $\sim 1.0$  mW to avoid heating. The excitation energies,  $E_L$ , (wavelengths,  $\lambda_L$ ) are Ti-Sapph 1.58 eV (785 nm), He-Ne 1.96 eV (632.8 nm), and  $Ar^+$  2.41 eV (514.5 nm).

Figure 1 plots the Raman spectra of five SLG samples exposed to different ion bombardment doses in the range  $10^{11}$   $Ar^+/cm^2$  (one defect per  $4 \times 10^4$  C atoms) to  $10^{15}$   $Ar^+/cm^2$  (one defect for every four C atoms). The bombardment procedure described in ref 28 is accurately reproducible. By tuning the bombardment exposure, we generated samples with  $L_D = 24, 14, 13, 7, 5,$  and  $2$  nm. All spectra in Figure 1 are taken at  $E_L = 2.41$  eV ( $\lambda_L = 514.5$  nm).

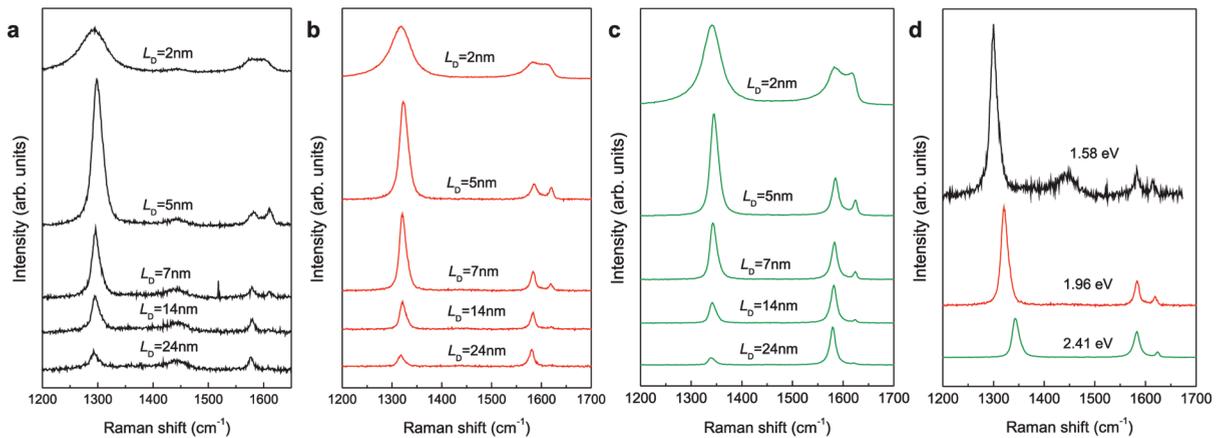
The Raman spectra in Figure 1 consist of a set of distinct peaks. The G and D appear around  $1580$  and  $1350$   $cm^{-1}$ , respectively. The G peak corresponds to the  $E_{2g}$  phonon at the Brillouin zone center. The D peak is due to the breathing modes of six-atom rings and requires a defect for its activation.<sup>4,18,19,39</sup> It comes from transverse optical (TO) phonons around the  $K$  or  $K'$  points in the first Brillouin zone,<sup>4,18,19</sup> involves an intervalley double resonance process,<sup>39,40</sup> and is strongly dispersive<sup>41</sup> with excitation energy due to a Kohn Anomaly at  $K$ .<sup>42</sup> Double resonance can also happen as intravalley process, i.e., connecting two points belonging to the same cone around  $K$  or  $K'$ .<sup>40</sup> This gives the so-called  $D'$  peak, which is centered at  $\sim 1620$   $cm^{-1}$  in defective samples measured at 514.5 nm.<sup>12</sup> The  $2D$  peak (also called  $G'$  in the literature) is the second order of the D peak.<sup>12,31</sup> This is a single peak in single layer graphene, whereas it splits in four in bilayer graphene, reflecting the evolution of the electron band structure.<sup>31,43</sup> The  $2D'$  peak (also called  $G''$  in analogy to  $G'$ ) is the second order of  $D'$ . Since  $2D(G')$  and  $2D'(G'')$  originate from a process where momentum conservation is satisfied by two phonons with opposite wavevectors, no defects are required for their activation, and are thus always present. On the other hand, the  $D + D'$  band ( $\sim 2940$   $cm^{-1}$ ) is the combination of phonons with different momenta, around  $K$  and  $\Gamma$ , thus requires a defect for its activation.

Reference 18 proposed a three stage<sup>44</sup> classification of disorder to simply assess the Raman spectra of carbons along an amorphization trajectory leading from graphite to tetrahedral amorphous carbon: (1) graphite to nanocrystalline graphite; (2) nanocrystalline graphite to low  $sp^3$  amorphous carbon; (3) low  $sp^3$  amorphous carbon to high  $sp^3$  (tetrahedral) amorphous carbon. In the study of graphene, stages 1 and 2 are the most relevant and are summarized here.

In stage 1, the Raman spectrum evolves as follows:<sup>18,28,29</sup> (a) D appears and  $I_D/I_G$  increases; (b)  $D'$  appears; (c) all peaks broaden. In the case of graphite the D and  $2D$  lose their doublet structure;<sup>18,46</sup> (e)  $D + D'$  appears; (f) at the end of stage 1, G and  $D'$  are so wide that they start to overlap. If a single Lorentzian is used to fit G and  $D'$ , this results in an upshifted wide G band at  $\sim 1600$   $cm^{-1}$ .

In stage 2, the Raman spectrum evolves as follows:<sup>18</sup> (a) the G peak position, denoted in the literature as  $Pos(G)$  or  $\omega_G$ , decreases from  $\sim 1600$   $cm^{-1}$  toward  $\sim 1510$   $cm^{-1}$ ; (b) the Tuinstra and Koenig relation fails and  $I_D/I_G$  decreases toward 0; (c)  $\omega_G$  becomes dispersive with the excitation laser energy, the dispersion increasing with disorder; (d) there are no more well-defined second-order peaks, but a broad feature from  $\sim 2300$  to  $\sim 3200$   $cm^{-1}$  modulated by the  $2D$ ,  $D + D'$ , and  $2D'$  bands.<sup>18,29</sup>

In disordered carbons  $\omega_G$  increases as the excitation wavelength decreases from IR to UV.<sup>18</sup> The dispersion rate,  $Disp(G) = \Delta\omega_G/\Delta E_L$ , increases with disorder. The G dispersion separates carbon materials into two types. In those with only  $sp^2$  rings,  $Disp(G)$  saturates at  $\sim 1600$   $cm^{-1}$ , the G position at the end of stage 1. In contrast, for those containing  $sp^2$  chains (such as in amorphous and diamondlike carbons), G continues to rise past



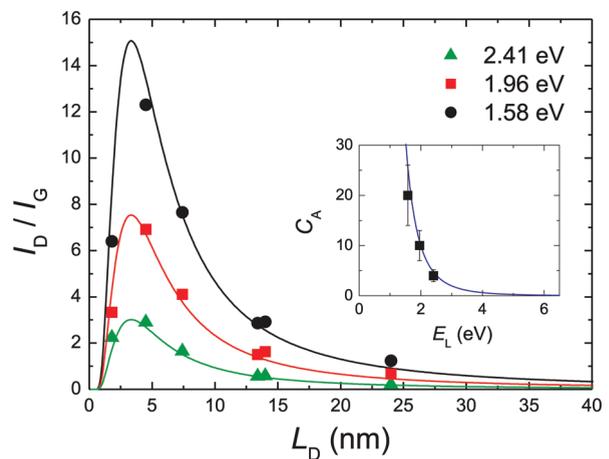
**Figure 2.** (a–c) Raman spectra of five ion-bombarded SLGs measured with  $E_L = 1.58$  eV ( $\lambda_L = 785$  nm),  $E_L = 1.96$  eV ( $\lambda_L = 632.8$  nm), and  $E_L = 2.41$  eV ( $\lambda_L = 514.5$  nm), respectively. (d) Raman spectra of an ion-bombarded SLG with  $L_D = 7$  nm obtained using these three excitation energies. The band  $\sim 1450$   $\text{cm}^{-1}$  in the Raman spectra at 785 nm is a third-order peak of the silicon substrate.<sup>33,47</sup>

1600  $\text{cm}^{-1}$  and can reach  $\sim 1690$   $\text{cm}^{-1}$  for 229 nm excitation.<sup>18,19</sup> On the other hand, D always disperses with excitation energy.<sup>18,19</sup>  $\Gamma_G$  always increases with disorder.<sup>10,24,28,29</sup> Thus, combining  $I_D/I_G$  and  $\Gamma_G$  allows one to discriminate between stages 1 or 2, since samples in stage 1 and 2 could have the same  $I_D/I_G$ , but not the same  $\Gamma_G$ , this being much bigger in stage 2.<sup>24,28,29</sup>

We note that Figure 1 shows the loss of sharp second order features in the Raman spectrum obtained from the  $L_D = 2$  nm SLG. This is an evidence that the range of defect densities in our study covers stage 1 (samples with  $L_D = 24, 14, 13, 7, 5$  nm) and the onset of stage 2 (sample with  $L_D = 2$  nm).

Figure 2a–c reports the first-order Raman spectra of our ion-bombarded SLGs measured at  $E_L = 1.58$  eV ( $\lambda_L = 785$  nm), 1.96 eV (632.8 nm), and 2.41 eV (514.5 nm), respectively. Figure 2d shows the Raman spectra of the ion-bombarded SLG with  $L_D = 7$  nm obtained using the three different laser energies. We note that  $I_D/I_G$  changes considerably with the excitation energy. This is a well-known effect in the Raman scattering of  $\text{sp}^2$  carbons.<sup>9,10,18,19,48,49</sup> Reference 10 noted that the integrated areas of different peaks depend differently on excitation energy  $E_L$ : while  $A_D$ ,  $A_{D'}$ , and  $A_{2D}$  shown no  $E_L$ -dependence,  $A_G$  was found to be proportional to  $E_L^4$ . The independence of  $A_{2D}$  on  $E_L$  agrees with the theoretical prediction<sup>50</sup> if one assumes that the electronic scattering rate is proportional to the energy. However, a fully quantitative theory is not trivial since, in general,  $A_D$  depends not only on the concentration of defects, but on their type as well (e.g., only defects able to scatter electrons between the two valleys  $K$  and  $K'$  can contribute).<sup>32–34</sup> Different defects can also produce different frequency and polarization dependence of  $A_D$ .<sup>32–34</sup>

Figure 3 plots  $I_D/I_G$  for all SLGs and laser energies. For all  $E_L$ ,  $I_D/I_G$  increases as  $L_D$  decreases (stage 1), reaches a maximum at  $L_D \sim 3$  nm, and decreases toward zero for  $L_D < 3$  nm (stage 2). It is important to understand what the maximum of  $I_D/I_G$  vs  $L_D$  means.  $I_D$  will keep increasing until the contribution from each defect sums independently.<sup>28,33</sup> In this regime (stage 1)  $I_D$  is proportional to the total number of defects probed by the laser spot. For an average defect distance  $L_D$  and laser spot size  $L_L$ , there are on average  $(L_L/L_D)^2$  defects in the area probed by the laser, thus  $I_D \propto (L_L/L_D)^2$ . On the other hand,  $I_G$  is proportional to



**Figure 3.**  $I_D/I_G$  for all SLGs and laser energies considered here. Solid lines are fits according to eq 1 with  $r_S = 1$  nm and  $r_A = 3.1$  nm. The inset plots  $C_A$  as a function of  $E_L$ . The solid curve is given by  $C_A = 160 E_L^4$ .

the total area probed by the laser ( $I_G \propto L_L^2$ ), giving  $I_D/I_G \propto 1/L_D^2$ .<sup>18,28</sup> However, if two defects are closer than the average distance an e-h pair travels before scattering with a phonon, then their contributions will not sum independently anymore.<sup>28,29,33,35</sup> This distance can be estimated as  $v_F/\omega_D \sim 3$  nm,<sup>33</sup> where  $v_F \sim 10^6$  m/s is the Fermi velocity around the  $K$  and  $K'$  points, in excellent agreement with the predictions of ref 33 and the data of refs 28, 29, and 35. For an increasing number of defects (stage 2), where  $L_D < 3$  nm,  $\text{sp}^2$  domains become smaller and the hexagons in the honeycomb lattice fewer and more distorted, until they open up. As the G peak is just related to the relative motion of  $\text{sp}^2$  carbons, we can assume  $I_G$  roughly constant as a function of disorder. Thus, with the loss of  $\text{sp}^2$  rings,  $I_D$  will decrease with respect to  $I_G$  and the  $I_D/I_G \propto 1/L_D^2$  relation will no longer hold. In this regime,  $I_D/I_G \propto M$  ( $M$  being the number of ordered hexagons), and the development of a D peak indicates ordering, exactly the opposite to stage 1.<sup>18</sup> This leads to a new relation:  $I_D/I_G \propto L_D^2$ .<sup>18</sup>

The solid lines in Figure 3 are fitting curves following the relation proposed in ref 28

$$\frac{I_D}{I_G} = C_A \frac{(r_A^2 - r_S^2)}{(r_A^2 - 2r_S^2)} [e^{-\pi r_S^2/L_D^2} - e^{-\pi(r_A^2 - r_S^2)/L_D^2}] \quad (1)$$

$r_A$  and  $r_S$  in eq 1 are length scales that determine the region where the D band scattering takes place.  $r_S$  determines the radius of the structurally disordered area caused by the impact of an ion.  $r_A$  is defined as the radius of the area surrounding the point defect in which the D band scattering takes place, although the  $sp^2$  hexagonal structure is preserved.<sup>28</sup> In short, the difference  $r_A - r_S$  defines the Raman relaxation length of the D band scattering and is associated with the coherence length of electrons that undergo inelastic scattering by optical phonons.<sup>28,35</sup> The fit in Figure 3 is done considering  $r_S = 1$  nm (as determined in ref 28 and expected to be a structural parameter, i.e.,  $E_L$  independent). Furthermore, within experimental accuracy, all data can be fit with the same  $r_A = 3.1$  nm, in excellent agreement with the values obtained in refs 28, 29, and 35. Any uncertainty in  $r_A$  does not affect the results in the low defect density regime ( $L_D > 10$  nm) discussed later.

Reference 28 suggested that  $I_D/I_G$  depends on both an activated (A) area, weighted by the parameter  $C_A$ , and a structurally defective area (S), weighted by a parameter  $C_S$ . Here we selected  $C_S = 0$  for two reasons: (i)  $C_S$  should be defect-structure dependent, and in the ideal case where the defect is the breakdown of the C–C bonds,  $C_S$  should be null; (ii) here we do not focus on the large defect density regime,  $L_D < r_S$ . The parameter  $C_A$  in eq 1 corresponds to the maximum possible  $I_D/I_G$ , which would be observed in the ideal situation where the D band would be activated in the entire sample, with no breakdown of any hexagonal carbon ring.<sup>28</sup>

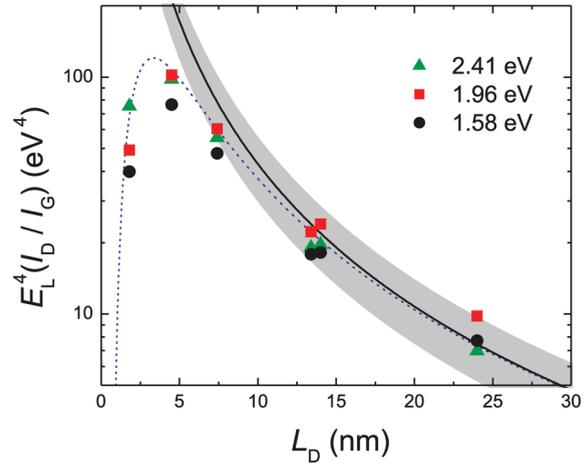
$C_A$  has been addressed in ref 28 as related to the ratio between the scattering efficiency of optical phonons between  $\mathbf{K}$  and  $\mathbf{\Gamma}$ . As we show here, the large  $I_D/I_G$  dependence on  $E_L$  comes from the change on  $C_A$ , which suggests this parameter might also depend on interference effects, when summing the different electron/hole scattering processes that are possible when accounting for the Raman cross section.<sup>51–55</sup> Note that  $C_A$  decreases as the laser energy increases. The solid line in the inset to Figure 3 is the fit of the experimental data (dark squares) by using an empirical relation between the maximum value of  $I_D/I_G$  and  $E_L$ , of the form  $C_A = AE_L^{-B}$ . The fit yields  $A = (160 \pm 48) \text{ eV}^4$ , by setting  $B = 4$  in agreement with refs 9 and 10.

We now focus on the low-defect density regime ( $L_D \geq 10$  nm), since this is the case of most interest in order to understand how Raman active defects limit the ultimate mobility of graphene samples.<sup>1–3</sup> In this regime, where  $L_D > 2r_A$ , the total area contributing to the D band scattering is proportional to the number of point defects, giving rise to  $I_D/I_G \propto 1/L_D^2$ , as discussed above. For large values of  $L_D$ , eq 1 can be approximated to

$$\frac{I_D}{I_G} \approx C_A \frac{\pi(r_A^2 - r_S^2)}{L_D^2} \quad (2)$$

By taking  $r_A = 3.1$  nm,  $r_S = 1$  nm, and also the relation  $C_A = (160 \pm 48)E_L^{-4}$  obtained from the fit of the experimental data shown in Figure 3, eq 2 can be rewritten as

$$L_D^2 \text{ (nm}^2\text{)} = \frac{(4.3 \pm 1.3) \times 10^3}{E_L^4} \left(\frac{I_D}{I_G}\right)^{-1} \quad (3)$$



**Figure 4.**  $E_L^4(I_D/I_G)$  as a function of  $L_D$  for the data shown in Figure 3. The dashed blue line is the plot obtained from the substitution of the relation  $C_A = (160)/E_L^{-4}$  in eq 1. The solid dark line is the plot of the product  $E_L^4(I_D/I_G)$  as a function of  $L_D$  according to eq 3. The shadow area accounts for the upper and lower limits given by the  $\pm 30\%$  experimental error.

In terms of excitation laser wavelength  $\lambda_L$  (in nanometers), we have

$$L_D^2 \text{ (nm}^2\text{)} = (1.8 \pm 0.5) \times 10^{-9} \lambda_L^4 \left(\frac{I_D}{I_G}\right)^{-1} \quad (4)$$

Equations 3 and 4 are valid for Raman data obtained from graphene samples with point defects separated by  $L_D \geq 10$  nm using excitation lines in the visible range. In terms of defect density  $n_D \text{ (cm}^{-2}\text{)} = 10^{14}/(\pi L_D^2)$ , eqs 3 and 4 become

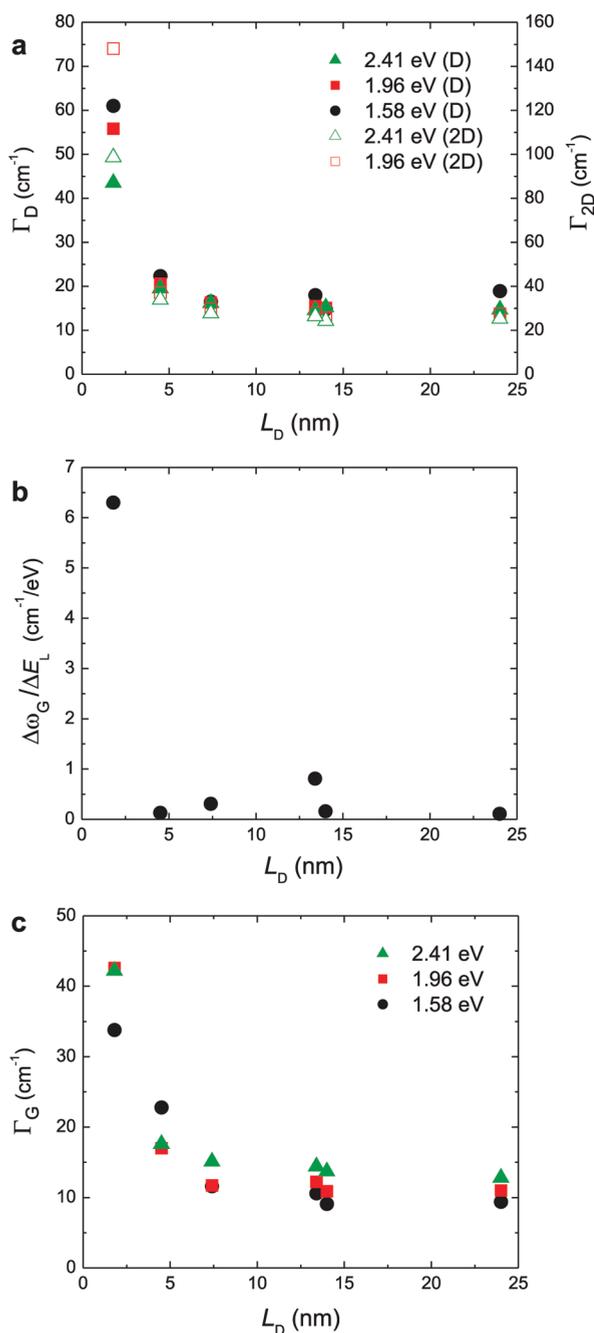
$$n_D \text{ (cm}^{-2}\text{)} = (7.3 \pm 2.2) \times 10^9 E_L^4 \left(\frac{I_D}{I_G}\right) \quad (5)$$

and

$$n_D \text{ (cm}^{-2}\text{)} = \frac{(1.8 \pm 0.5) \times 10^{22}}{\lambda_L^4} \left(\frac{I_D}{I_G}\right) \quad (6)$$

Figure 4 plots  $E_L^4(I_D/I_G)$  as a function of  $L_D$  for the data shown in Figure 3. The data with  $L_D > 10$  nm measured with different laser energies collapse in the same curve. The dashed blue line is the plot obtained from the substitution of the relation  $C_A = (160)/E_L^4$  in eq 1. The solid dark line is the plot  $E_L^4(I_D/I_G)$  versus  $L_D$  according to eqs 3 and 4. The shadow area accounts for the upper and lower limits given by the  $\pm 30\%$  experimental error. The plot in Figure 4 validates these relations for samples with  $L_D > 10$  nm.

Although these relations are based on the Raman spectra of ion-bombarded samples, they should be valid for other types of point defects (e.g., resonant scatterers, substitutional atoms) in the limit of large  $L_D$ , where the nature of the defect should not have a strong influence on the  $I_D/I_G$  ratio. Indeed a similar evolution of the Raman spectra can be seen in ref 27. However, eqs 3–6 are of course limited to Raman active defects. For example, perfect zigzag edges,<sup>32–34</sup> charged impurities,<sup>58–60</sup> intercalants,<sup>61</sup> and uniaxial and biaxial strain<sup>62,63</sup> do not generate a D peak. For these types of “silent” defects, other Raman signatures can be used. A perfect zigzag edge does change the



**Figure 5.** (a) Plot of  $\Gamma_D$  and  $\Gamma_{2D}$  versus  $L_D$ . (b) G peak dispersion [ $\text{Disp}(G) = \Delta\omega_G/\Delta E_L$ ] as a function of  $L_D$ .  $\Delta\omega_G/\Delta E_L$  remains zero until the onset of stage 2. (c) FWHM(G) =  $\Gamma_G$  as a function of  $L_D$ . As suggested in refs 24 and 29,  $\Gamma_G$  remains roughly constant until the onset of the second stage of amorphization, corresponding to the maximum  $I_D/I_G$ .

G peak shape,<sup>64,65</sup> while strain, intercalants, and charged impurities have a strong influence on the G and 2D peaks.<sup>58–62</sup>

Figure 5a plots  $\Gamma_D$  and  $\Gamma_{2D}$  as a function of  $L_D$ . Within the experimental error, a dependence of  $\Gamma_D$  or  $\Gamma_{2D}$  on the excitation energy during stage 1 cannot be observed. D and 2D always disperse with excitation energy, with  $\Delta\omega_D/\Delta E_L \sim 52 \text{ cm}^{-1}/\text{eV}$ , and  $\Delta\omega_{2D}/\Delta E_L = 2\Delta\omega_D/\Delta E_L$ .

Figures 5b,c plot the G peak dispersion  $\text{Disp}(G) = \Delta\omega_G/\Delta E_L$  and  $\Gamma_G = \text{FWHM}(G)$  as a function of  $L_D$ , respectively. As shown

in Figure 5b,  $\Delta\omega_G/\Delta E_L$  remains zero until the onset of stage two, when it becomes slightly dispersive ( $\Delta\omega_G/\Delta E_L \sim 6 \text{ cm}^{-1}/\text{eV}$ ).  $\Gamma_G$  (Figure 5c) remains roughly constant at  $\sim 14 \text{ cm}^{-1}$ , a typical value for as-prepared exfoliated graphene,<sup>11,31,56,57</sup> until the onset of stage 2 (corresponding to the maximum  $I_D/I_G$ ) as suggested in ref 24 and shown in ref 29 for a single laser line  $E_L = 2.41 \text{ eV}$ . Combining  $I_D/I_G$  and  $\Gamma_G$  allows to discriminate between stages 1 or 2, since samples in stage 1 and 2 could have the same  $I_D/I_G$ , but not the same  $\Gamma_G$ , which is much larger in stage 2.<sup>24,29</sup>

In summary, we discussed the use of Raman spectroscopy to quantify the amount of pointlike defects in graphene. We used different excitation laser lines in ion-bombarded samples in order to measure their respective  $I_D/I_G$ . We find that  $I_D/I_G$ , for a specific  $L_D$ , depends on the laser energy. We presented a set of empirical relations that can be used to quantify point defects in graphene samples with  $L_D > 10 \text{ nm}$  via Raman spectroscopy using any laser line in the visible range. We show that the Raman coherence length  $r_A$  is  $E_L$ -independent, while the strong  $E_L$  dependence for  $I_D/I_G$  comes from the parameter  $C_A$ .<sup>28</sup> By definition, our analysis only applies to defects able to activate the D peak in the Raman process. Some defects do not give rise to the D peak but change other Raman peaks and peaks intensities; other defects are altogether Raman silent. In this case, the combination of Raman spectroscopy with other independent probes of the number of defects in a sample can provide a wealth of information on the nature of such defects.

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